

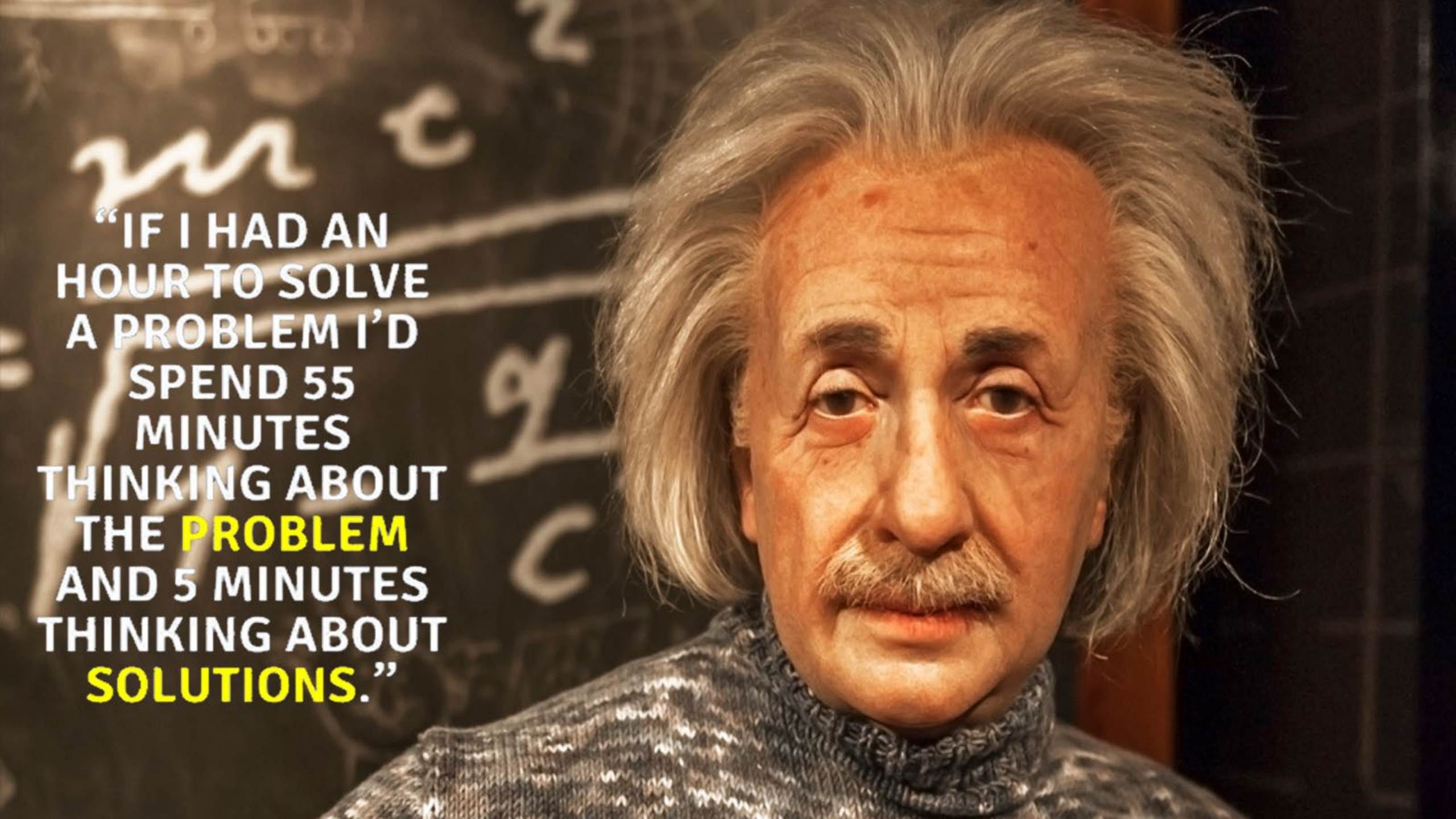
QGP: A Novel Quantum Good Privacy for Enhanced Security, Privacy, and Authentication

Paul Wang, Ph.D.



Morgan Quantum Computing Group

- Computing, Cryptology, Cryptography, and Security



“IF I HAD AN
HOUR TO SOLVE
A PROBLEM I'D
SPEND 55
MINUTES
THINKING ABOUT
THE **PROBLEM**
AND 5 MINUTES
THINKING ABOUT
SOLUTIONS.”

Color



Vulnerabilities



Cybersecurity

Buffer overflow
Injection attacks



Artificial Intelligence/ Machine Learning

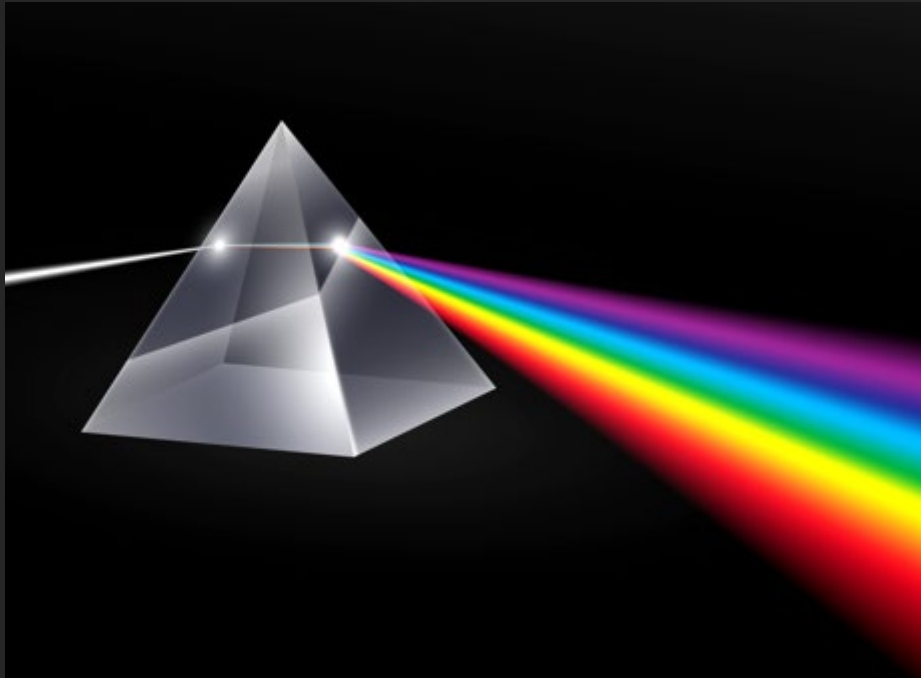
Non-bias, equitable, responsible
ethical, trustworthy



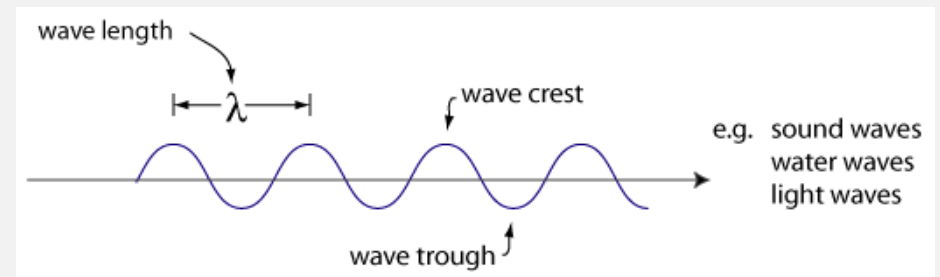
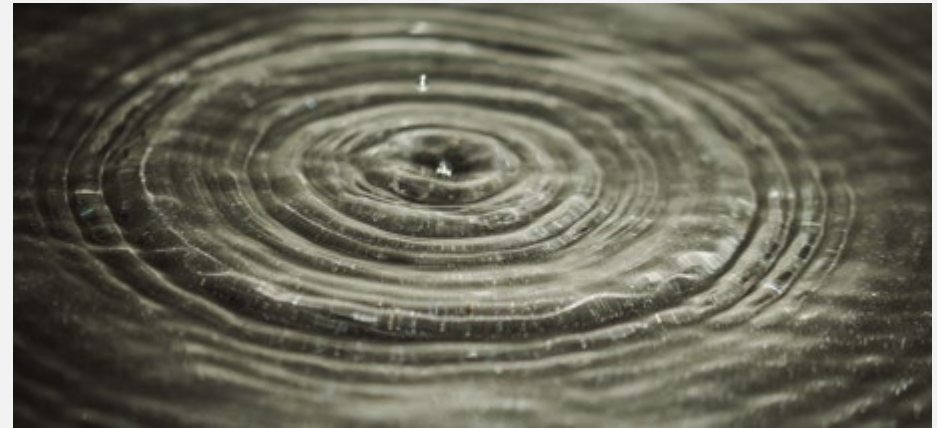
Secure Coding

Bugs
Logic flaws
Exploitable

Light, *Quantum Theory of*



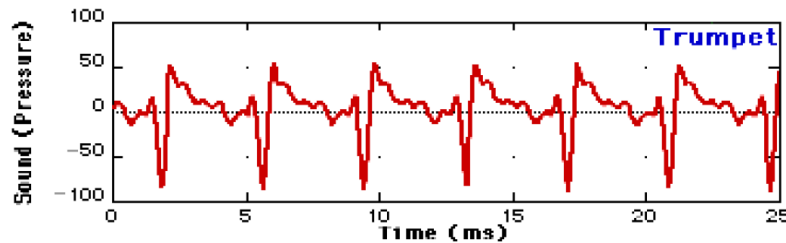
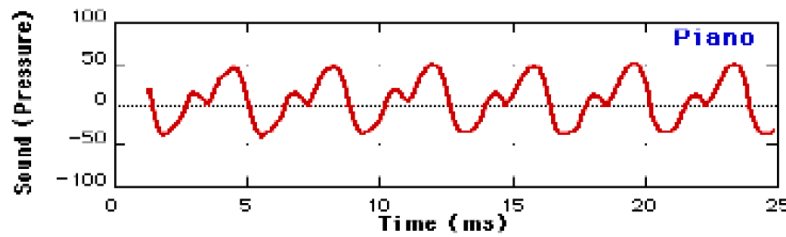
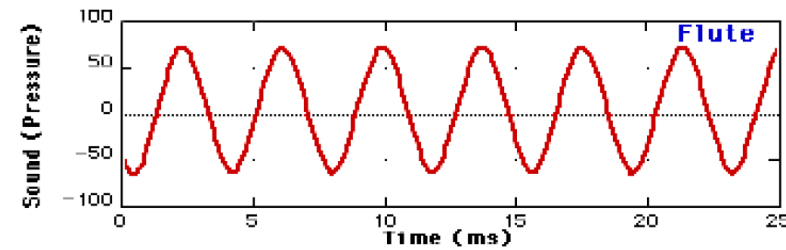
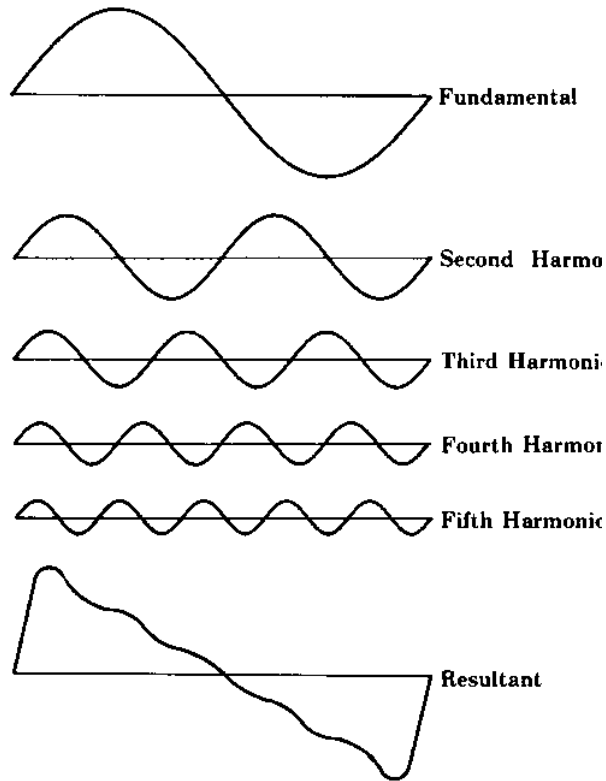
- **Light** is composed of particles called **photons**.
- **Matter** is composed of particles called electrons, **protons**, and neutrons.
- It's only when the mass of a particle gets small enough that its **wavelike** properties show up.



In the 1600s, Christiaan Huygens, a Dutch physicist, showed that light behaves like a **wave**.

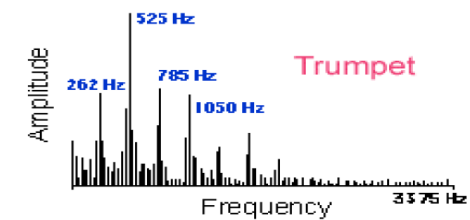
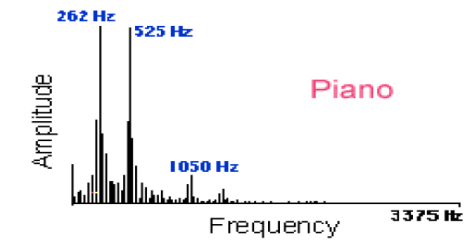
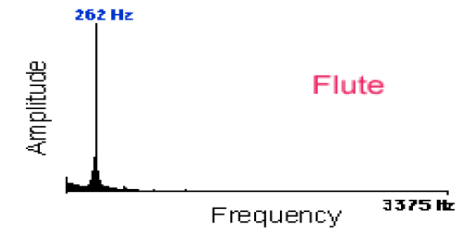
Waves – Cycles

Karaoke, Voice Cancellation



$$262 \text{ Hz} = (440 * \sqrt[12]{2} * \sqrt[12]{2} * \sqrt[12]{2}) / 2$$

note C



Period and Transform

Clock

Piano, 7, 12, 26, 400

Pi or e (??)

XOR

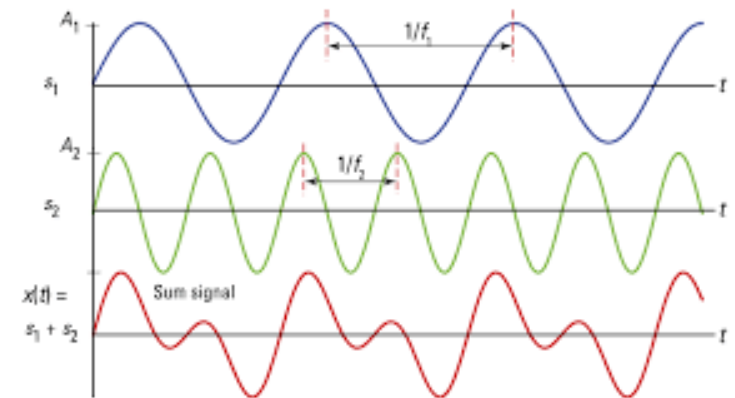
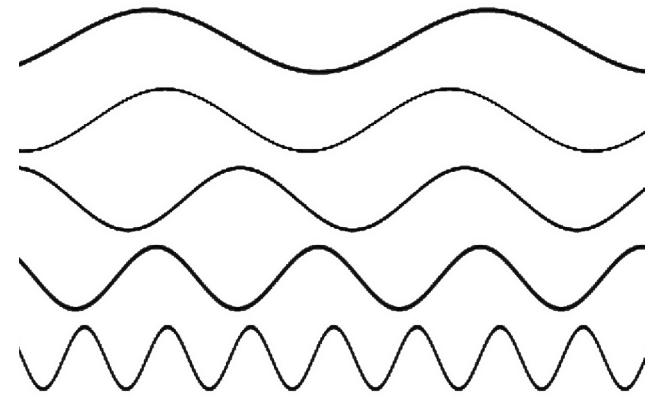
$$9 + 6 = 3 \quad \text{mod } 12$$

$$3 + 6 = 9 \quad \text{mod } 12$$

$$5 + 3 = 2 \quad \text{mod } 7$$

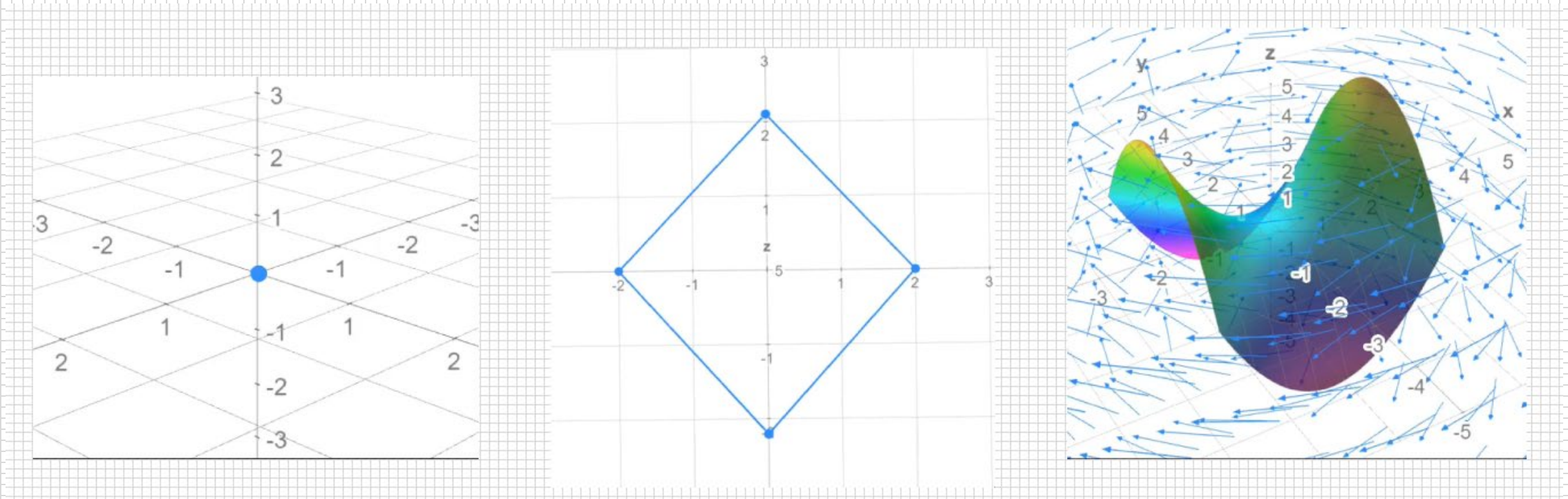
$$25 + 2 = 1 \quad \text{mod } 26$$

$$e^{ix} = \cos x + i \sin x,$$





The Beauty of Transform

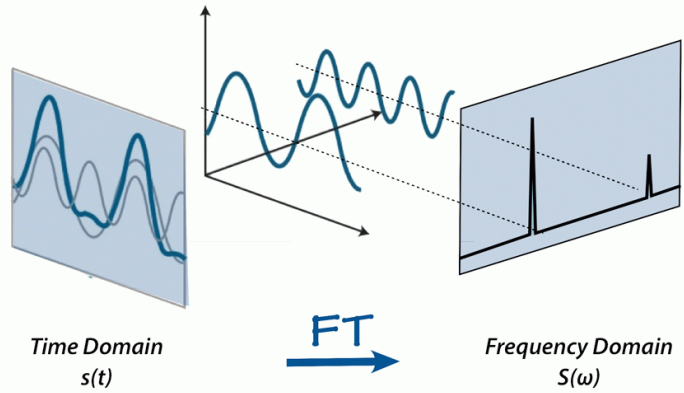


A point or a line?

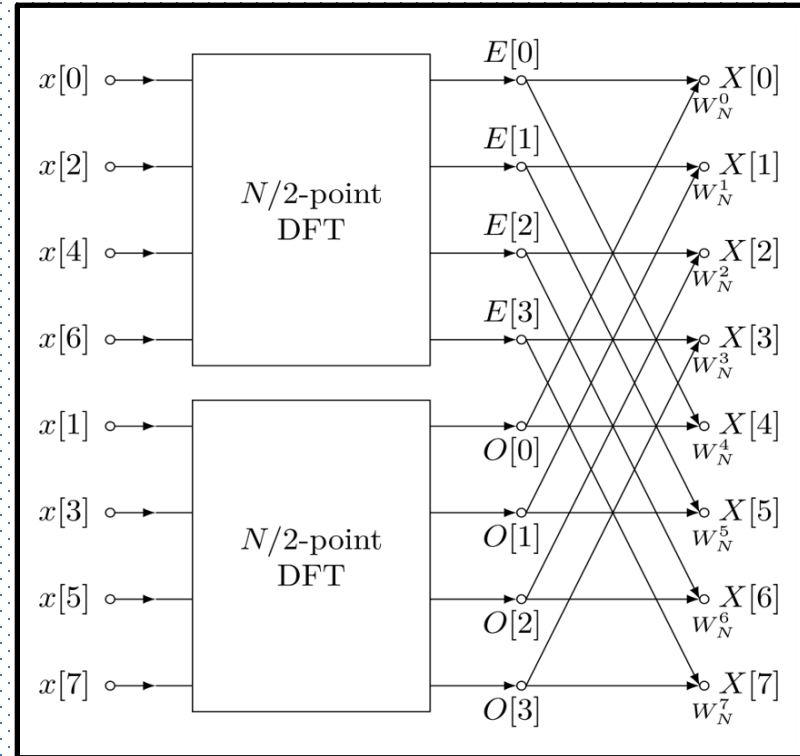
2D or 3D space?

Random or patterns?

The Beauty of Transform – FFT



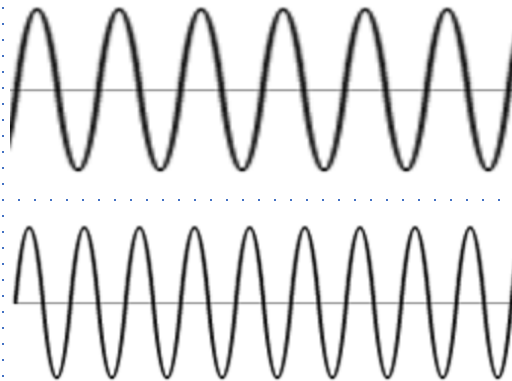
N -point
DFT



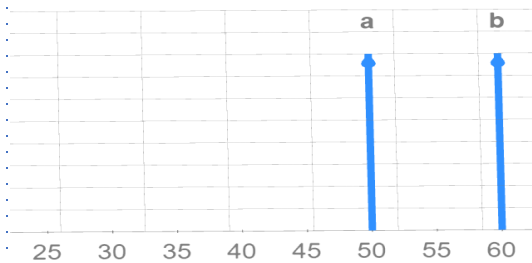
Butterfly

Recursion!

Time Domain



Frequency Domain



A FFT algorithm on $n = 2^p$ inputs with respect to a primitive n -th root

of unity $\omega_n^k = e^{-\frac{2\pi i k}{n}}$ relies on

$O(n \log_2 n)$ butterflies of add & sub

Shor's Algorithm

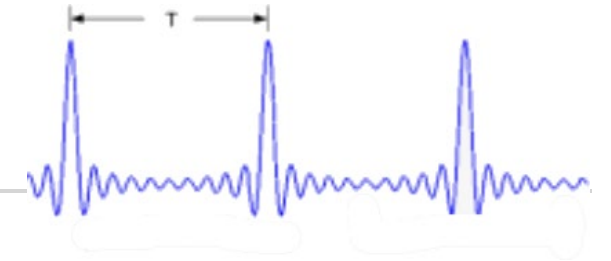
- Shor's algorithm, 1994
- Implementation
 - 15 = 3x5, 2001 and 2012
 - 21 in 2019
 - 35 failed due to errors

```
In [1]: N = 10403
        for x in range (2, N):
            for y in range (2, N):
                if x*y == N:
                    print ("x=", x, "y=", y)
```

```
x= 101 y= 103
x= 103 y= 101
```

- The core is factoring sth. like $x^2 = (x+1)(x-1) = 0 \pmod N$
 - **Period**
 - **Transform**

Period in RSA Algorithm



Modular
Exponentiation:

$$f(x) = a^x \pmod{N}$$

where $a \neq p, q$ is an integer number, the modulus $N = pq$

Number Theory:

$f(x)$ is periodic with period r .

Period:

$$r = (p - 1)(q - 1) \quad \text{Hard if finding } r \text{ from only } N - \text{order finding}$$

Key Pair:

Public key: e, N ; Private key: d, N

e Satisfies:

$$3 \leq e \leq N - 1, \quad \gcd(e, r) = 1 \text{ (coprime)}$$

d = Inverse e :

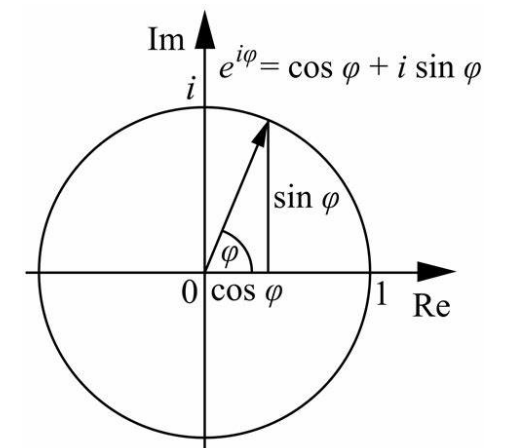
$$d = e^{-1} \pmod{r}$$

Encryption:

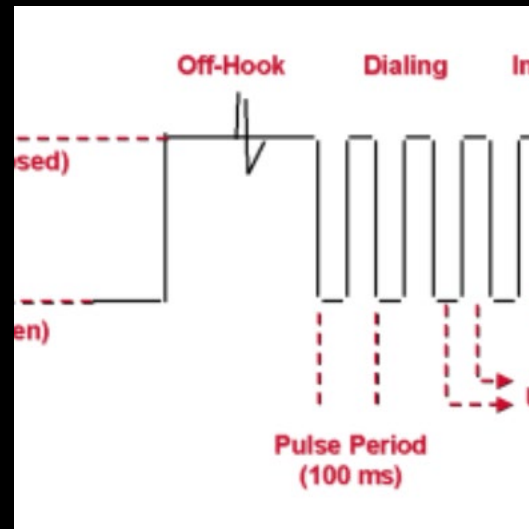
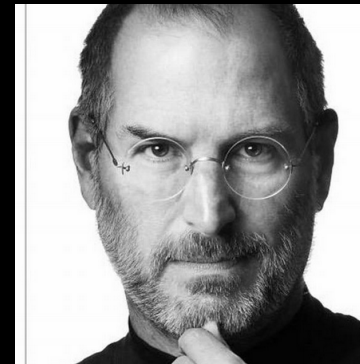
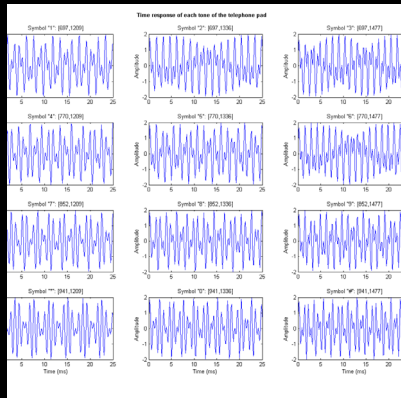
$$c = m^e \pmod{N}$$

Decryption:

$$c^d \pmod{N} = (m^e)^d \pmod{N} = m$$



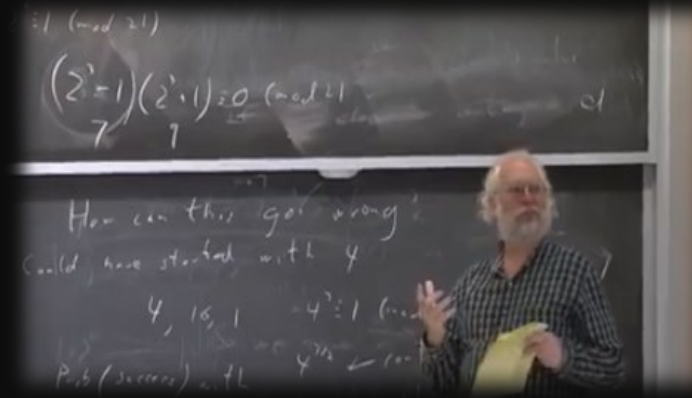
Bluebox vs. “Greenbox”



Shor: exponential speed up,
mathematically

of qubits?

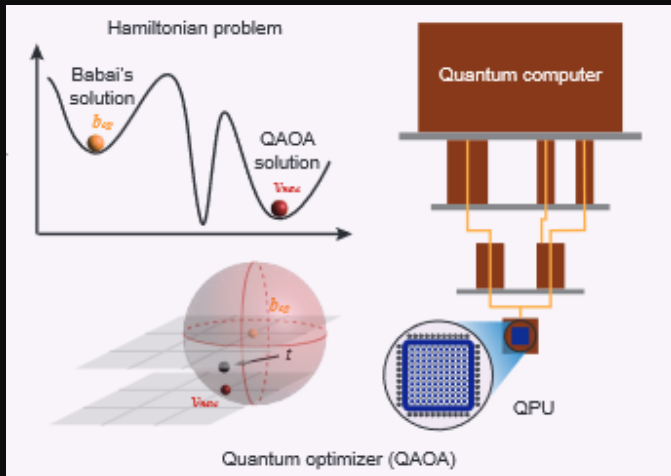
Circuit depth?



RSA 2048: 372 qubits with thousands
of depth

- IBM: 127 qubits, 433 qubits

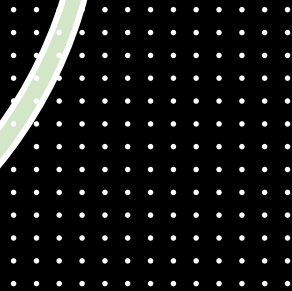
<https://arxiv.org/abs/2212.12372>



How Secure Are We Now?



RSA Backdoor?



How much trust to the third party?

Key-Splitting

A key can be crafted using modular arithmetic such that a third party can decipher without requiring the private key.

Could this have been already embedded in RSA?

An **exercise** for interested people.

[A new idea for RSA backdoors \(arxiv.org\)](https://arxiv.org/abs/1607.01714)

[How the NSA \(may have\) put a backdoor in RSA's cryptography: A technical primer \(cloudflare.com\)](https://www.cloudflare.com/learning/ssl/how-the-nsa-may-have-put-a-backdoor-in-rsa-cryptography-a-technical-primer/)

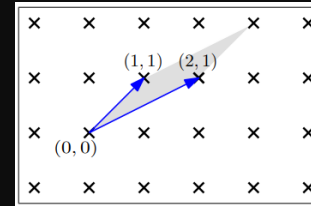
[Report: NSA Paid RSA \\$10M to Create 'Back Door' in Encryption Software | PCMag](https://www.pcmag.com/news/2013/08/20/nsa-paid-rsa-10m-to-create-back-door-in-encryption-software/)

Encryptions and Key Establishment

CRYSTALS-Kyber

Asymmetric Algorithm

Module Lattice, LWE (Learning With Errors) Based



\mathbb{R}^2 vs. \mathbb{R}^{400}

Digital Signatures

CRYSTALS-Dilithium-AES

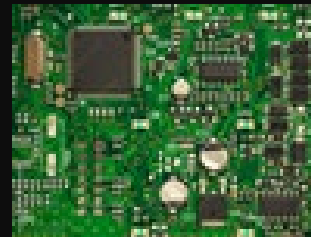
Asymmetric Algorithm



Side-Channel Attacks

Timing Attacks, Power, Electromagnetic, Fault Attacks

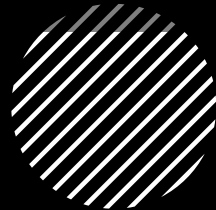
RISC-V PQC ISA



Post Quantum Cryptography



Worry Free !?



Worry Free With PQC?

Enigma: needs 100 years to break – T/F?

- Statistical analysis

DES – 1976

- 3DES to store government document to 2030 – T/F?
- DES cracker – 1998, NSA involvement, AES – 2002

RSA – 1977

- 300 trillion years to break RSA-2048 – T/F?
- Never been approved for no short cut
- Vulnerable to quantum attacks

PQC – 2023

- Secure against any computers – T/F?

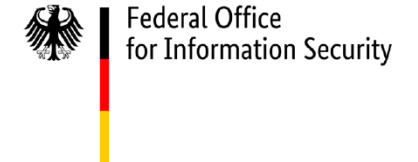
Worrisome QKD

French Cybersecurity Agency (ANSSI)

Federal Office for Information Security (BSI)

Netherlands National Communications Security Agency (NLNCSA)

Swedish National Communications Security Authority, Swedish Armed Forces



General Intelligence and
Security Service
Ministry of the Interior and
Kingdom Relations



- Need for specialized hardware and high costs
 - Single photon sources and detectors
 - Eavesdropping, interference → DoS
- Distance limitations and end-to-end security
 - Currently hundreds km
 - Need **trusted nodes** for longer distance, thus **end-to-end** vulnerable
 - Key rate is limited. Satellite?
- Reliance on classical cryptography for peer authentication
 - Authentication: pre-shared keys must be present at both ends before running QKD protocol
 - The secret key must be distributed and then periodically renewed in a secure manner

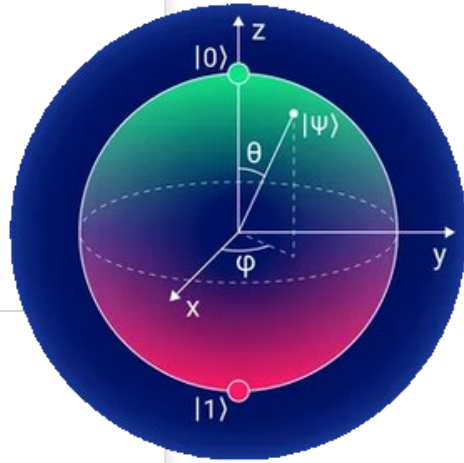


Mistakes Made in History



What we thought was a strong crypto algorithm may not be that strong when looking from a **new** perspective.

QFT Speed Up



Initialization

Recursion

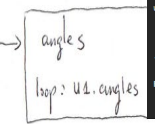
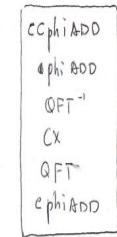
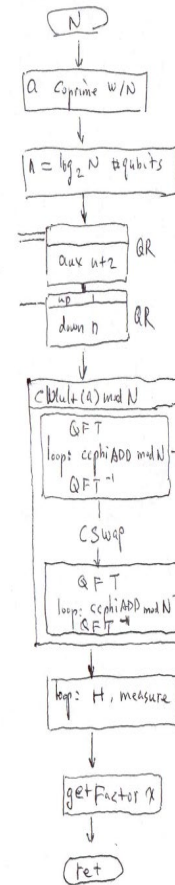
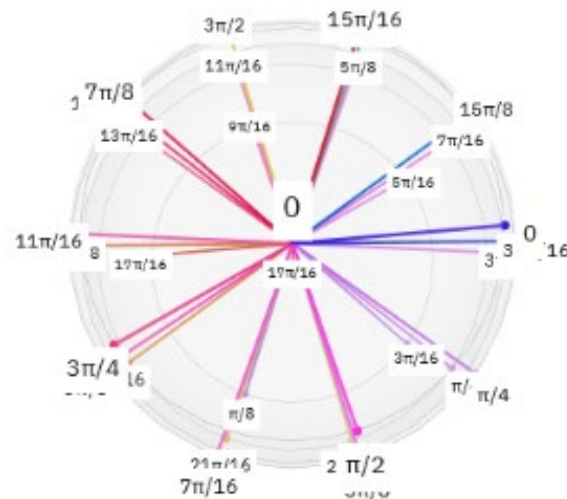
QFT

Modular ADD (phi)

QFT⁻¹

Measure

Calculate factors



```

from qiskit.aqua import QuantumInstance
from qiskit.aqua.algorithms import Shor

provider = IBMQ.load_account()

#IBMQ.enable_account()
# '2048804aa2f176b72fcb2a374dec492241766d16c4b1010100f62c2370419d04f260f50b8950a33'
#provider = IBMQ.get_provider(auth='ibmq-')

backend = provider.get_backend('ibmq_peek_simulator') # Specifies the quantum device
#backend = Aer.get_backend('qasm_simulator')
# backend = provider.get_backend('ibmq_16_melbourne') # using quantum backend

print('\n Shors Algorithm')
print('-----')
print('\nExecuting...\n')

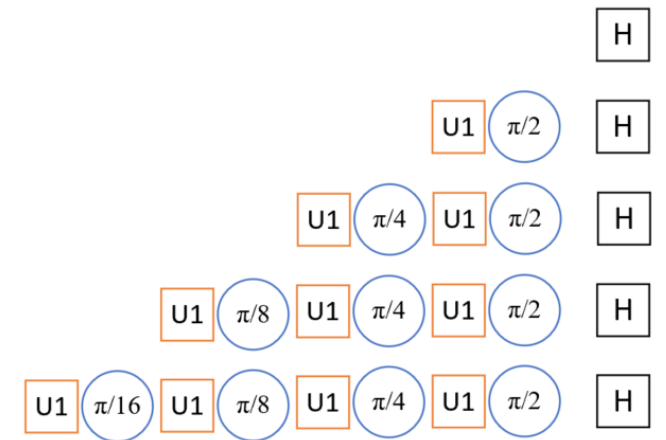
factors = Shor(N) #function to run Shor's algorithm

result_dict = factors.run(QuantumInstance(backend, shots=10, skip_qobj_validation=False))
result = result_dict['factors'] # Get factors from results

print(result)

/opt/conda/lib/python3.8/site-packages/qiskit/providers/ibmq/ibmqfactory.py:192: UserWarning:
erties, jobs, and job results are all now in local time instead of UTC.
warnings.warn(Timestamps in IBMQ backend properties, jobs, and job results '
ibmqfactory.load_account:WARNING:2021-02-17 01:45:28,330: Credentials are already in use. The
will be replaced.

Shors Algorithm
-----
Executing...
[[5, 7]]
    
```



Exp to Add/Sub With Additional Polynomial Overhead

Quantum Computing

Superposition



```
For each apple on the apple tree  
  if color == green then continue  
  else "red apple found"
```

Entanglement



Interferences





Why Binary?

Base 2 vs. Base N



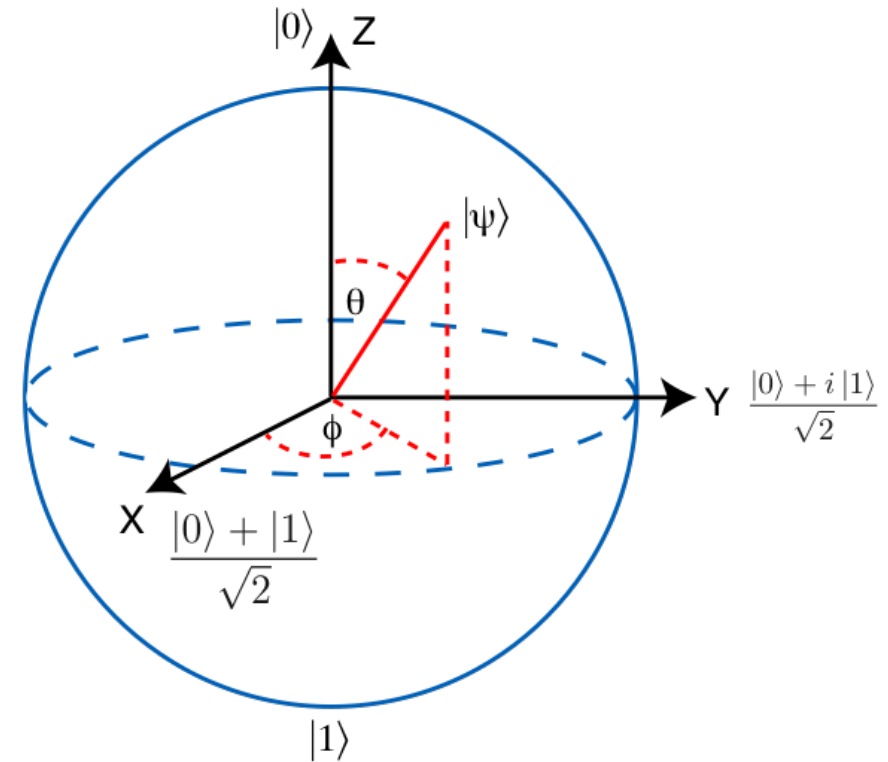
π music



Creative
Commons

O(time) Analysis

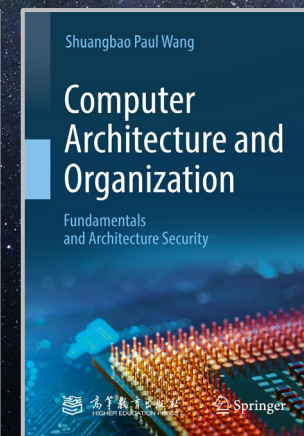
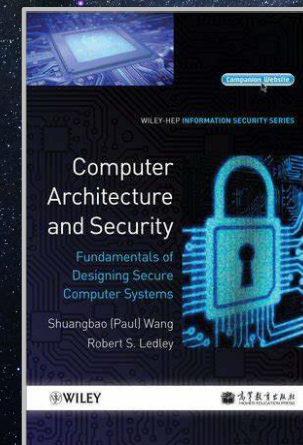
- 1D time domain signal
 - Compress/stretch a signal in time domain: **hard**
 - Compress/stretch in frequency domain: easy
- 2D time domain signal
 - Process in time domain: **slow** ($n \times n$ for image processing)
 - Process in frequency domain: fast ($n \log n$)
- e^x (nD) time domain signal
 - **Impossible** to process due to time
 - QFT to frequency domain to perform add/sub

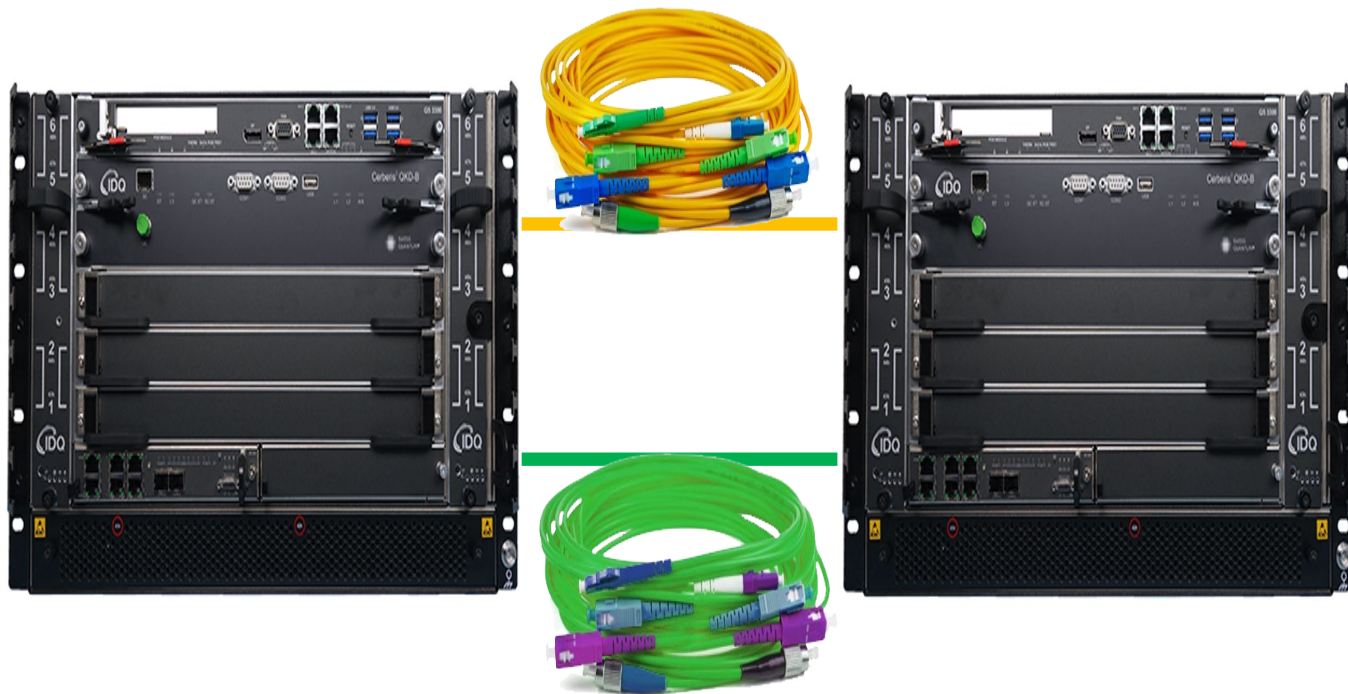
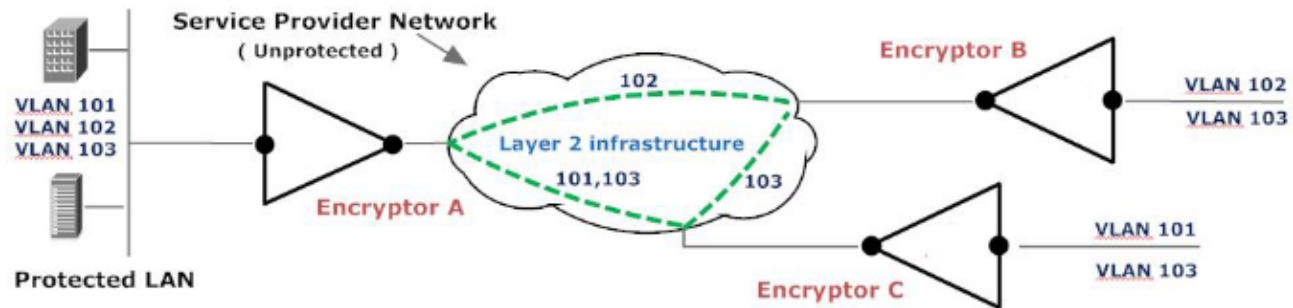


Quantum Internet

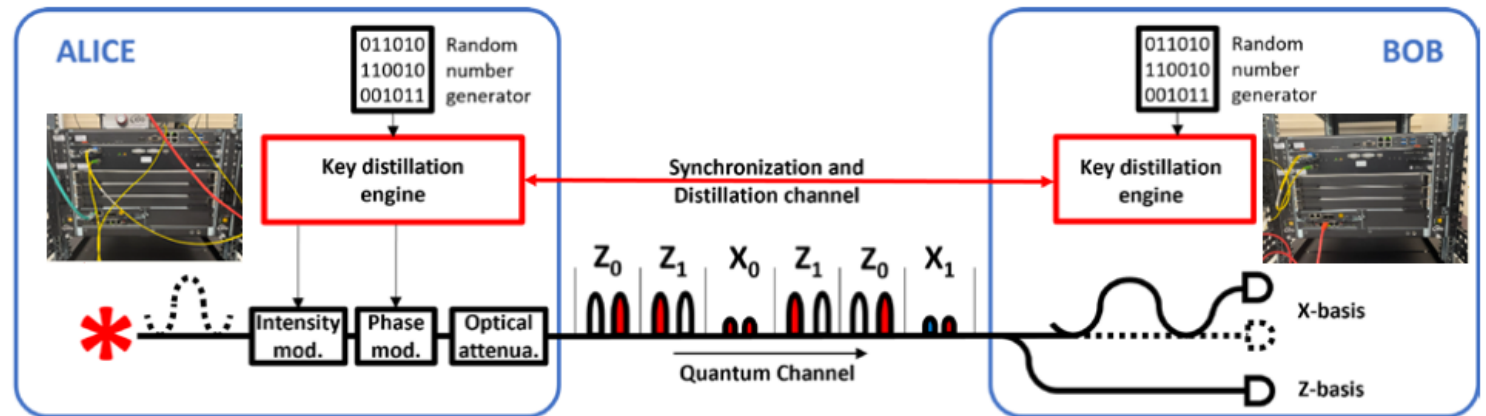
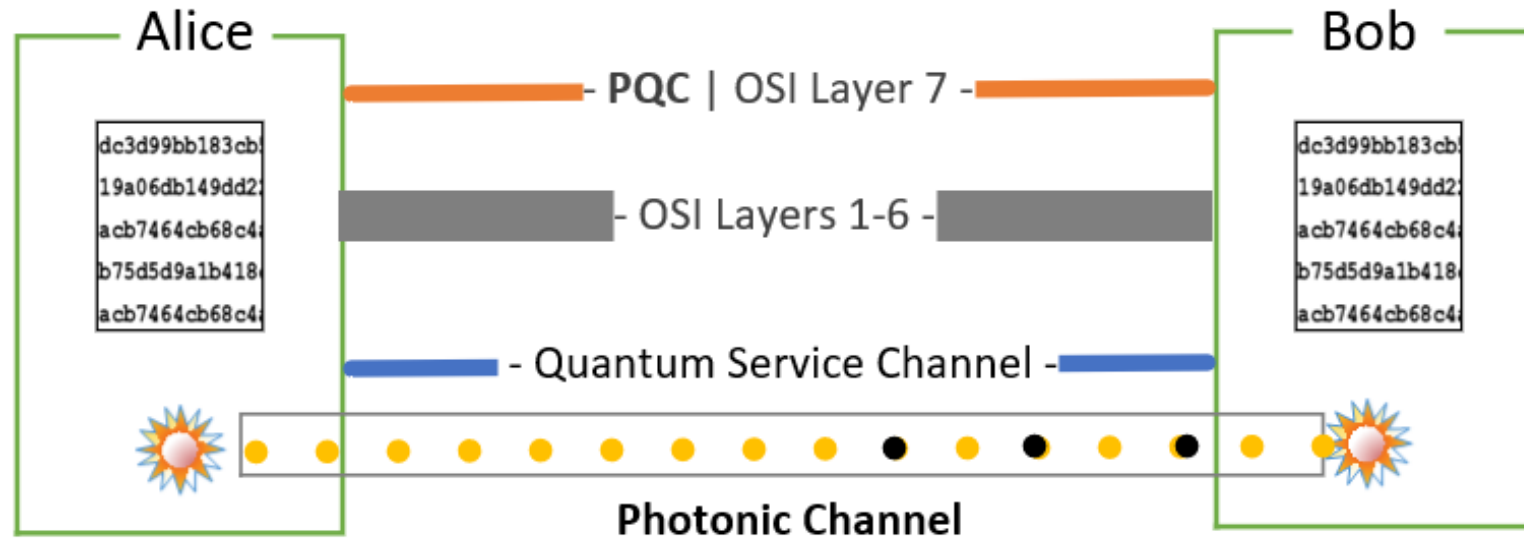
- Networking protocol: TCP/IP
 - 7 layers: APSTNDP
- Routers and switches
 - Quantum memory
- Encryption key distribution
 - Asymmetric key encryption (RSA)
 - Digital signatures

Security Enhancement

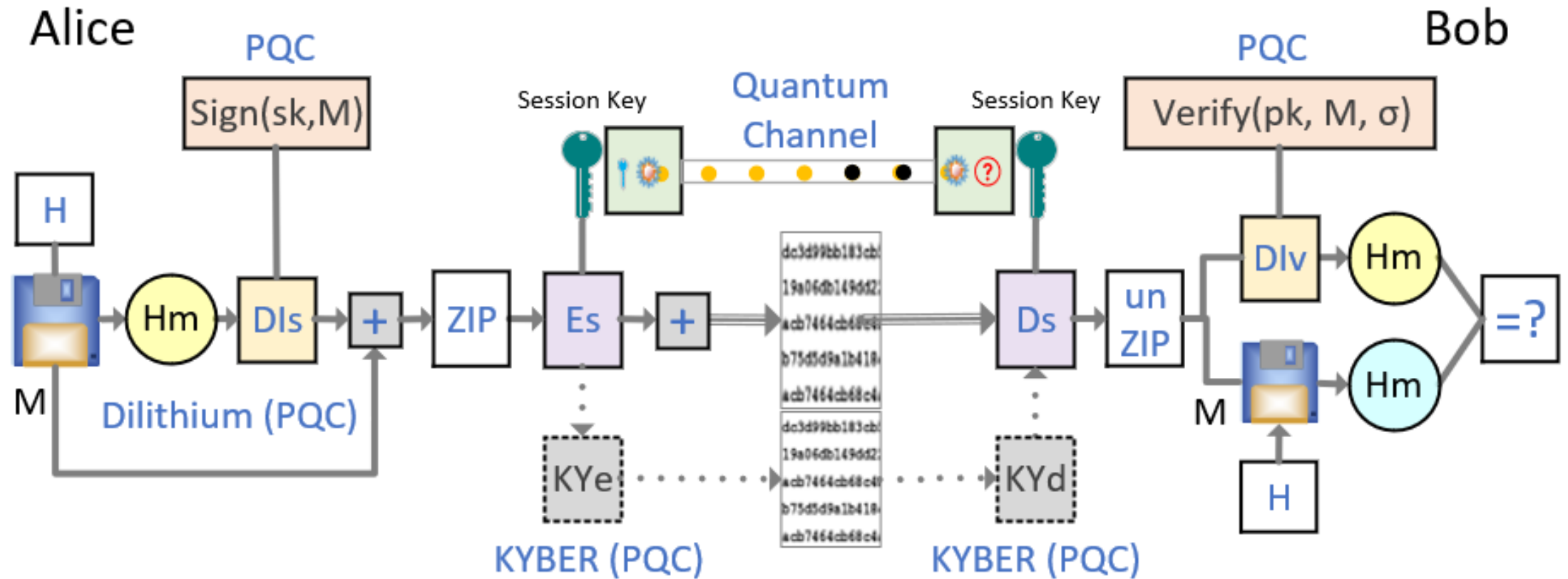




Adding Layer 0 and Modified Layer 7



QGP – Quantum Good Privacy



To Build a
Quantum
Internet Testbed

Quantum
computing is
the future

Quantum
cryptography
is now



“Cyber attacks present the greatest threat to our national and economic security today, and the magnitude of the threat is growing. This bill is an important step toward curbing these dangerous cyber attacks.”

Senate Intelligence Committee
Cybersecurity Bill – 2014



Paul Wang
<https://www.linkedin.com/in/paulwangedu>

